Issue partial fractioning with GiNaC

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1 Introduction

Let us investigate here, when the function of GiNaC, sqrfree parfrac gives wrong results.

I first noticed this error, for terms of the form

$$\frac{1}{a}\frac{x^b}{(x-1)^c}\,.\tag{1}$$

Applying this to some particular example, using partial fractioning this should give

$$\frac{1}{4}\frac{x^4}{x-1} = \frac{1}{4}\left(x^3 + x^2 + x + \frac{1}{x-1} + 1\right).$$
(2)

The result outputed by GiNaC was

$$\frac{1}{4}\left(x^3 + x^2 + x + 1\right) + \frac{1}{x - 1}.$$
(3)

As you can see, the prefactor missing in front of the $\frac{1}{x-1}$ term is missing. That this is not simply an output error can be seen from plugging a value for the x term, here I used x = 4.

I investigated this and the following terms all give wrong result.

$$\frac{1}{4} \frac{x^4}{(x-1)^2} \,, \tag{4}$$

$$\frac{1}{4}\frac{x^3}{(x-1)^3}\,,\tag{5}$$

$$\frac{1}{3}\frac{x^3}{(x-1)^2}\,,\tag{6}$$

$$\frac{1}{5}\frac{x^2}{(x-1)^3}\,.$$
(7)

Notice however, that terms of the form (no denominator present for the numerical prefactor) give a correct result:

$$3\frac{x^3}{(x-1)^2}\,.$$
(8)

As you can see, there is an emerging pattern. We always see that the term 1/(...) initially present in the expression is missing the (numerical) prefactor, if the prefactor is a ratio.

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The code I used was
#include <iostream>
#include <complex>
#include <math.h>
#include <ginac/ginac.h>
using std::cout;
using std::endl;
int main()
{
    GiNaC::symbol x("x");
    GiNaC:: ex ex1 = pow(x,4)/(x-1)/4;
    GiNaC:: ex ex2 = GiNaC:: sqrfree_parfrac(ex1, x);
    cout \ll "the input is ex1 = " \ll ex1 \ll endl;
    cout << "the result after partial fractioning: "<< ex2 << endl;
    cout \ll "this is what you get after x=4, in ex1 = "\ll ex1.subs(x==4)\ll endl;
    cout << "insert number:, say x = 4, which gives wrong result "
    << ex2.subs(x==4) << endl;
```

}

And I modified the term ex1 accordingly.